

## MTH 1125 - Test 2

SUMMER 2023

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Name \_\_\_\_\_

**Instructions.** Show CLEARLY how you arrive at your answers.

1. Compute:  $\frac{d}{dx} [6x^6 + 9x^4 - 12x^3 + 18x^2 + 8x + 4\sqrt{x} + 2] =$

2. Compute:  $\frac{d}{dx} [(6x^4 + 8x^3 + 5)(3x^2 + 6x + 2)] =$

3. Compute:  $\frac{d}{dx} \left[ \frac{10x^3 + 15x^2 + 10x + 2}{2x^2 + 8x} \right] =$

4. Compute:  $\frac{d}{dx} [(6x^4 + 12x^2 + 7)^5] =$

5. Given that  $f(x) = 4x^2 - 7x + 4$ , write the *equation* of the line tangent to the graph of  $f(x)$  at the point  $(2, 6)$ .

6. Given that  $v = \sin(w)$  and that  $w = x^3 + 3x$ ; compute  $\frac{dv}{dx}$  **using the Leibniz form of the Chain Rule.** (In particular, when doing this exercise, *write explicitly the Leibniz form of the chain rule that you are going to use.*)

7. Compute:  $\frac{d}{dx} [\sec(\sin(x))]$  =

8. Compute:  $\frac{d}{dx} \left[ \left( \frac{3x^4 + 6x^2 + 3}{\cos(x) + 4x^2} \right)^{20} \right]$  =

9. Compute:  $\frac{d}{dx} [\cos^3 (2x^2 + 4x + 5)] =$

10. Given that  $3y^2 + 6x^3y^5 + 2x^5 = \tan (y)$ , compute  $\frac{dy}{dx}$

11. Given that  $f(x) = 2x^2 + 6x + 7$ , compute  $f'(x)$  **using the definition of derivative.**  
(i.e., using the “limit process.”)

**Extra** (Wow! 10 Points)

Given that  $L'(x) = \frac{2x+6}{x^2+6x+5}$  (i.e.,  $\frac{d}{dx} [L(x)] = \frac{2x+6}{x^2+6x+5}$ ); compute  $\frac{d}{dx} [L(\tan(x))]$  =