

# MTH 1125 (2 pm - Pod A) Test #3

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Name \_\_\_\_\_

**Instructions.** Show CLEARLY how you arrive at your answers.

1.  $f(x) = 2x^3 + 3x^2 + 2$  Determine the intervals on which  $f(x)$  is increasing/decreasing and identify all relative maximums and minimums. (Caution - there are **two** critical numbers. Make sure you get them both!)

2.  $f(x) = \frac{1}{4}x^4 + 2x^3 - \frac{15}{2}x^2 + 6x + 3$  Determine the intervals on which  $f(x)$  is Concave up/Concave down and identify all points of inflection.

3.  $f(x) = x^3 + 6x^2 - 15x + 3$  on the interval  $[-2, 2]$ . Find the Absolute Maximum and Absolute Minimum values (if they exist).

4.  $f(x) = x^{\frac{20}{7}} - \frac{10}{3}x^{\frac{6}{7}} + 4$  Determine the intervals on which  $f(x)$  is increasing/decreasing and identify all relative maximums and minimums.

5. A rectangle is inscribed in the region bounded by the positive  $x$ -axis, the positive  $y$ -axis, and the graph of  $f(x) = (x - 7)^6$  as shown below. Determine the value of  $x$  that makes the area of the rectangle as large as possible.

**REMARK:** When you create the area function  $A(x)$ , **do not simplify (i.e. “multiply it out”)** before you compute the derivative. If you simplify (i.e. “multiply it out”) the area function  $A(x)$  before you compute the derivative, it will be very difficult to find the critical numbers.

