

MTH 1125 - Test 2 (12pm Class)

FALL 2023

Pat Rossi

Name _____

Instructions. Show CLEARLY how you arrive at your answers.

1. Compute: $\frac{d}{dx} [8x^5 + 10x^4 + 8x^3 + 12x^2 + 12x + 24\sqrt{x} + 10] =$

2. Compute: $\frac{d}{dx} [(\sin(x) + \cos(x))(8x^5 + 4x + 2)] =$

3. Compute: $\frac{d}{dx} \left[\frac{3x^5 + 5x^3 + 15x}{4x^2 + 8} \right] =$

4. Compute: $\frac{d}{dx} [(3x^3 + 6x^2 + 15x)^{10}] =$

5. Given that $f(x) = 2x^2 - 3x + 2$, give the *equation* of the line tangent to the graph of $f(x)$ at the point $(2, 4)$.

6. Given that $w = \cos(u)$ and that $u = 4t^2 + 2t + 2$; compute $\frac{dw}{dt}$ **using the Leibniz form of the Chain Rule**. (In particular, when doing this exercise, *write explicitly the Leibniz form of the chain rule that you are going to use.*)

7. Compute: $\frac{d}{dx} [\sec(8x^5 + 5x^2)] =$

8. Compute: $\frac{d}{dx} \left[\left(\frac{3x^2 + 12x}{4x^2 + 8x + 16} \right)^8 \right] =$

9. Compute: $\frac{d}{dx} [\cos^8 (x^4 + 2x^2)] =$

10. Given that $5x^4 - x^4y^4 = \cos (y)$, compute $\frac{dy}{dx}$

11. Given that $f(x) = 5x^2 - 6x + 2$, compute $f'(x)$ **using the definition of derivative.**
(i.e., using the “limit process.”)

Extra (Wow! 10 Points)

Given that $S'(x) = \frac{1}{\sqrt{1-x^2}}$ (i.e., $\frac{d}{dx} [S(x)] = \frac{1}{\sqrt{1-x^2}}$); compute $\frac{d}{dx} [S(\cos(x))]$